

$$y = -\frac{29}{81}e^{2t} + \frac{2}{27}te^{2t} - \frac{1}{9}t^2e^{2t} + \frac{1}{9}t^3e^{2t} + \frac{29}{81}e^{-t} \Big|_{t=0} = 0$$